anisotropic thermal-motion behaviour of the equatorial and apical F atoms was interpreted as the consequence of a probable tilting of the chains along the $c$ axis (Babel \& Knoke, 1978); such behaviour is also observed for $\mathrm{Pb}_{2} \mathrm{MnFe}_{2} \mathrm{~F}_{12} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ with the apical $F(2)$ and equatorial $F(3)$ strongly distributed in the $a b$ plane and in the $\mathbf{c}$ direction (see $U_{i j}$, Table 1) respectively. Nevertheless, as usual, the terminal $F$ atom $\mathrm{F}(1)$ corresponds to a shorter $M-\mathrm{F}$ distance than the bridging ones $[\mathrm{F}(2), \mathrm{F}(3)$ ]. Although H atoms have not been located, the $\mathrm{O}(w)-\mathrm{F}(3)$ distance, distinctly shorter than the other $\mathrm{O}(w)-\mathrm{F}$ distances (Table 2), suggests that hydrogen bonding may occur through $\mathrm{F}(3)$; thus the H atom could occupy an $(x 0 z) 6(i)$ position with $x \simeq 0.35, z \simeq 0.30$. Another related material showing triangular isolated octahedral chains is $\mathrm{KCrF}_{4}$ (Dewan \& Edwards, 1986; Kissel \& Hoppe, 1987). Thermal behaviour and magnetic properties are now being investigated. Possible isotypic materials are being researched.

The authors are very indebted to Dr M. Leblanc (Université du Maine) for the X-ray data collection.

## References

Babel, D. \& Knoke, G. (1978). Z. Anorg. Allg. Chem. 442, 151-162.
Dewan, J. C. \& Edwards, A. J. (1986). J. Chem. Soc. Dalton. Trans. 12, 2623-2627.
Fourquet, J. L., Plet, F., Courbion, G., Bulou, A. \& De Pape, R. (1979). Rev. Chim. Minér. 16, 490-500.

Kissel, D. \& Hoppe, Z. (1987). Z. Naturforsch. Teil B, 42, 135-141.
Le Bail, A. \& Mercier, A. M. (1991). Eur. J. Solid State Inorg. Chem. In the press.
Lösch, R. \& Hebeker, C. H. (1979). Z. Naturforsch. 346, 131-134.
Plet, F., Fourquet, J. L., Courbion, G., Leblanc, M. \& De Pape, R. (1979). J. Cryst. Growth, 47, 699-702.
Shannon, R. D. (1976). Acta Cryst. A32, 751-767.
Sheldrick, G. M. (1976). SHELX76. A program for crystal structure determination. Univ. of Cambridge, England.
Suzuki, T. (1960). Acta Cryst. 13, 279-281.

# Crystal Chemistry of cyclo-Hexaphosphates. XIX. Structure of Barium cyclo-Hexaphosphate Octahydrate 

By Mohamed Rzaigu<br>Ecole Normale Supérieure, 7021 Zarzouna Bizerte, Tunisia<br>and Marie-Thérèse Averbuch-Pouchot and André Durif<br>Laboratoire de Cristallographie, associé à l'Université J. Fourier, CNRS, 166X, 38042 Grenoble CEDEX, France

(Received 11 June 1991; accepted 22 August 1991)


#### Abstract

Ba}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .8 \mathrm{H}_{2} \mathrm{O}, \quad M_{r}=1029.966\), monoclinic, $\quad C 2 / c, \quad a=20.98$ (2), $\quad b=7.227$ (3),$\quad c=$ 17.44 (1) $\AA, \beta=119.56$ (3) ${ }^{\circ}, V=2300(5) \AA^{3}, Z=4$, $D_{x}=2.974 \mathrm{Mg} \mathrm{m}^{-3}, \quad \lambda(\mathrm{Mo} \mathrm{K} \mathrm{\alpha})=0.7017 \AA, \quad \mu=$ $5.764 \mathrm{~mm}^{-1}, F(000)=1928, T=294 \mathrm{~K}$, final $R=$ 0.041 for 2699 reflections. The atomic arrangement can be described as being built of two layers of $\mathrm{BaO}_{8}$ and $\mathrm{BaO}_{10}$ polyhedra approximately centred by planes $z=\frac{1}{4}$ and $\frac{3}{4}$ interconnected through the external oxygen atoms of the large $\mathrm{P}_{6} \mathrm{O}_{18}$ groups. Inside a layer the Ba polyhedra assemble to form rings of eight polyhedra tiling the plane. The phosphoric ring anion has a twofold internal symmetry rarely observed in the crystal chemistry of cyclohexaphosphates. Hydrogen atoms could not be located.


Introduction. From a structural point of view very little is known about divalent cation cyclo-hexaphosphates. The chemical preparation and crystal structure of the cadmium salt, $\mathrm{Cd}_{3} \mathrm{P}_{6} \mathrm{O}_{18} \cdot 6 \mathrm{H}_{2} \mathrm{O}$, were first reported by Averbuch-Pouchot (1989a), later on the chemical preparation and characterization of the isotypic manganese salt were described by AverbuchPouchot \& Durif (1989). The chemical preparation and crystal structure of the copper salt, $\mathrm{Cu}_{3^{-}}$ $\mathrm{P}_{6} \mathrm{O}_{18} .14 \mathrm{H}_{2} \mathrm{O}$, have also been reported by AverbuchPouchot (1989b). Some chemical investigations by Lazarevski, Kubasova, Chudinova \& Tananaev (1980, 1982a,b) showing the existence of several hydrated compounds, $\mathrm{Cd}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .16 \mathrm{H}_{2} \mathrm{O}$, $\mathrm{Mn}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .9 \mathrm{H}_{2} \mathrm{O}, \mathrm{Co}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .14 \mathrm{H}_{2} \mathrm{O}, \mathrm{Ni}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .17 \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Cu}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .14 \mathrm{H}_{2} \mathrm{O}$, should also be mentioned. The
© 1992 International Union of Crystallography
crystallographic investigation of the copper salt by Averbuch-Pouchot (1989b) confirms the hydration state reported by these authors. In addition, from the powder data given by these same authors it can be concluded that, in spite of a similar degree of hydration, the cobalt and copper salts are not isotypic.

Experimental. Two processes can be used to prepare the title compound. The first one consists of adding an aqueous solution of barium chloride in small fractions to an aqueous solution of lithium cyclohexaphosphate. A white precipitate appears at each addition but dissolves on stirring. The two aqueous solutions are used in stoichiometric proportions. The resulting solution is slowly evaporated at room temperature until the title compound crystallizes. In the second process an excess of solid barium hydroxide is added and cyclo-hexaphosphoric acid itself is produced through the use of ion-exchange resins (Amberlite IR120). The so-obtained mixture is then filtered and the resulting solution evaporated at room temperature.

Crystal size $0.12 \times 0.12 \times 0.18 \mathrm{~mm}$. Density not measured. Philips PW 1100 diffractometer, graphite monochromator. 18 reflections $\left(9.70<\theta<11.20^{\circ}\right)$ for refining unit-cell dimensions. $\omega$ scan, scan width $1.20^{\circ}$, scan speed $0.02^{\circ} \mathrm{s}^{-1}$, total background measuring time 6 s . 3119 reflections collected ( $3<\theta<$ $\left.32.50^{\circ}\right), \pm h, k, l: h_{\max }=31, k_{\max }=11, l_{\max }=22$. Two orientation and intensity control reflections ( $\overline{5} 11$ and $\overline{5} 11)$ measured every 6 h without any significant variation. Lorentz and polarization corrections, no absorption correction.

The crystal structure was solved using direct methods (MULTAN77; Main, Lessinger, Woolfson, Germain \& Declercq, 1977) for the location of the heavy atoms and successive Fourier syntheses. Hydrogen atoms were not located. Anisotropic fullmatrix least-squares refinement (on $F$ ); unit weights. Scattering factors for neutral atoms and $f^{\prime}, f^{\prime \prime}$ from International Tables for X-ray Crystallography (1974, Vol. IV, Table 2.2B). Enraf-Nonius (1977) SDP used for all calculations. Computer used MicroVAX II. No secondary-extinction correction. The results are for final refinements with 2699 reflections $[I>3 \sigma(I)]$. Final $R=0.041(w R=0.047), S=3.330$, maximum $\Delta / \sigma=0.0$, maximum peak height in the final difference Fourier synthesis $=0.76 \mathrm{e} \AA^{-3}$. Table 1 reports the final atomic coordinates for this atomic arrangement.*

[^0]Table 1. Final atomic coordinates and $B_{\text {eq }}$ values for $\mathrm{Ba}_{3} \mathrm{P}_{6} \mathrm{O}_{18} \cdot 8 \mathrm{H}_{2} \mathrm{O}$
E.s.d.'s are given in parentheses.

$$
B_{e q}=\frac{4}{3} \sum_{i} \sum_{j} \mathbf{a}_{i \cdot} \cdot \mathbf{b}_{j} \beta_{i j}
$$

|  | $x$ | $y$ | $z$ | $B_{\text {eq }}\left(\AA^{2}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Ba}(1)$ | $0.29249(2)$ | $0.89119(5)$ | $0.71863(2)$ | $1.059(6)$ |
| $\mathrm{Ba}(2)$ | 0 | $0.26714(8)$ | $\frac{3}{4}$ | $1.121(9)$ |
| $\mathrm{P}(1)$ | $0.12812(8)$ | $0.8848(2)$ | $0.7833(1)$ | $0.94(3)$ |
| $\mathrm{P}(2)$ | $0.46599(8)$ | $0.8279(3)$ | $0.3701(1)$ | $1.08(3)$ |
| $\mathrm{P}(3)$ | $0.37650(8)$ | $0.1503(2)$ | $0.5828(1)$ | $0.99(3)$ |
| $\mathrm{O}(L 13)$ | $0.3733(3)$ | $0.3394(7)$ | $0.6286(3)$ | $1.41(9)$ |
| $\mathrm{O}(E 11)$ | $0.3130(2)$ | $0.2796(7)$ | $0.7222(3)$ | $1.34(9)$ |
| $\mathrm{O}(E 12)$ | $0.3743(3)$ | $0.5911(7)$ | $0.7222(3)$ | $1.7(1)$ |
| $\mathrm{O}(E 21)$ | $0.4431(3)$ | $-0.0167(7)$ | $0.8343(3)$ | $1.5(1)$ |
| $\mathrm{O}(E 22)$ | $0.4351(3)$ | $0.2565(9)$ | $0.9222(3)$ | $1.9(1)$ |
| $\mathrm{O}(L 23)$ | $0.4472(2)$ | $0.8127(8)$ | $0.0725(3)$ | $1.4(1)$ |
| $\mathrm{O}(E 31)$ | $0.3873(3)$ | $0.0068(7)$ | $0.1425(3)$ | $1.6(1)$ |
| $\mathrm{O}(E 32)$ | $0.3138(3)$ | $0.1509(8)$ | $0.4908(3)$ | $1.5(1)$ |
| $\mathrm{O}(L 12)$ | $0.4513(2)$ | $0.3101(7)$ | $0.7903(3)$ | $1.34(9)$ |
| $\mathrm{O}(W 1)$ | $0.1979(2)$ | $0.5914(8)$ | $0.6366(3)$ | $1.51(9)$ |
| $\mathrm{O}(W 2)$ | $0.2206(3)$ | $0.1019(9)$ | $0.0265(4)$ | $2.5(1)$ |
| $\mathrm{O}(W 3)$ | $0.1658(3)$ | $0.8670(9)$ | $0.1343(4)$ | $2.1(1)$ |
| $\mathrm{O}(W 4)$ | $0.4432(4)$ | $0.361(1)$ | $0.0767(4)$ | $3.1(2)$ |
|  |  |  |  |  |

Table 2. Main interatomic distances $(\AA)$ and bond angles $\left({ }^{\circ}\right)$ in the atomic arrangement of $\mathrm{Ba}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .8 \mathrm{H}_{2} \mathrm{O}$
E.s.d.'s are given in parentheses.
$\mathrm{P}_{6} \mathrm{O}_{18}$ anion

| $\mathrm{P}_{6} \mathrm{O}_{18}$ $\mathrm{P}(1) \mathrm{O}_{4}$ | nion <br> etrahedro |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(1)$ | $\mathrm{O}(13)$ | $\mathrm{O}(E 11)$ | $\mathrm{O}(E 12)$ | $\mathrm{O}(\mathrm{L} 12)$ |
| $\mathrm{O}(\mathrm{L13})$ | 1.586 (6) | 2.547 (9) | 2.437 (8) | 2.475 (6) |
| $\mathrm{O}(E 11)$ | 111.6 (3) | 1.493 (6) | 2.593 (7) | 2.544 (6) |
| $O(E 12)$ | 104.6 (3) | 120.5 (3) | 1.494 (5) | 2.500 (7) |
| $\mathrm{O}(\mathrm{L12})$ | 101.3 (3) | 109.9 (3) | 107.1 (3) | 1.614 (4) |
| $\mathrm{P}(2) \mathrm{O}_{4}$ tetrahedron |  |  |  |  |
| P (2) | $\mathrm{O}(E 21)$ | $\mathrm{O}(E 22)$ | $\mathrm{O}(23)$ | $\mathrm{O}(L 12)$ |
| $\mathrm{O}(E 21)$ | 1.478 (5) | 2.556 (9) | 2.534 (6) | 2.515 (8) |
| $\mathrm{O}(E 22)$ | 119.3 (4) | 1.484 (7) | 2.477 (8) | 2.515 (9) |
| $\mathrm{O}(223)$ | 111.2 (3) | 107.3 (3) | 1.592 (4) | 2.454 (6) |
| $\mathrm{O}(\mathrm{L} 12)$ | 108.8 (3) | 108.6 (3) | 99.9 (3) | 1.613 (6) |
| $\mathrm{P}(3) \mathrm{O}_{4}$ tetrahedron |  |  |  |  |
| $\mathrm{P}(3)$ | $\mathrm{O}(L 13)$ | $\mathrm{O}(223)$ | $\mathrm{O}($ E31) | $\mathrm{O}(E 32)$ |
| $\mathrm{O}(L 13)$ | 1.602 (6) | 2.463 (9) | 2.517 (7) | 2.496 (7) |
| $\mathrm{O}(223)$ | 100.5 (3) | 1.601 (6) | 2.559 (9) | 2.448 (6) |
| $\mathrm{O}(E 31)$ | 109.4 (3) | 112.2 (3) | 1.481 (6) | 2.580 (7) |
| $\mathrm{O}(E 32)$ | 107.6 (3) | 104.7 (3) | 120.5 (3) | 1.490 (4) |


| $\mathrm{P}(1)-\mathrm{O}(L 12)-\mathrm{P}(2)$ | $125.2(4)$ | $\mathrm{P}(1)-\mathrm{P}(2)$ | $2.865(2)$ |
| :--- | :---: | :--- | :--- |
| $\mathrm{P}(2)-\mathrm{O}(L 23)-\mathrm{P}(3)$ | $138.9(4)$ | $\mathrm{P}(2)-\mathrm{P}(3)$ | $2.990(2)$ |
| $\mathrm{P}(3)-\mathrm{O}(L 13)-\mathrm{P}(1)$ | $133.3(4)$ | $\mathrm{P}(3)-\mathrm{P}(1)$ | $1.926(3)$ |
| $\mathrm{P}(2)-\mathrm{P}(1)-\mathrm{P}(3)$ | $98.95(7)$ |  |  |
| $\mathrm{P}(1)-\mathrm{P}(2)-\mathrm{P}(3)$ | $116.38(9)$ |  |  |
| $\mathrm{P}(1)-\mathrm{P}(3)-\mathrm{P}(2)$ | $102.55(6)$ |  |  |


| $\mathrm{Ba}(1) \mathrm{O}_{10}$ polyhedron |  |  |  |
| :--- | :--- | :--- | :--- |
| $\mathrm{Ba}(1)-\mathrm{O}(E 11)$ | $2.836(5)$ | $\mathrm{Ba}(1)-\mathrm{O}(E 31)$ | $2.978(7)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(E 11)$ | $2.978(6)$ | $\mathrm{Ba}(1)-\mathrm{O}(W 1)$ | $2.806(5)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(E 12)$ | $2.748(5)$ | $\mathrm{Ba}(1)-\mathrm{O}(W 1)$ | $2.830(6)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(E 21)$ | $2.865(4)$ | $\mathrm{Ba}(1)-\mathrm{O}(W 2)$ | $2.919(6)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(W 3)$ | $2.934(6)$ | $\mathrm{Ba}(1)-\mathrm{O}(W 3)$ | $2.902(6)$ |
| $\mathrm{Ba}(2) \mathrm{O}_{8}$ polyhedron |  |  |  |
| $\mathrm{Ba}(2)-\mathrm{O}(E 12)$ | $2.746(6)(\times 2)$ | $\mathrm{Ba}(2)-\mathrm{O}(E 31)$ | $2.720(5)(\times 2)$ |
| $\mathrm{Ba}(2)-\mathrm{O}(E 21)$ | $2.785(6)(\times 2)$ | $\mathrm{Ba}(2)-\mathrm{O}(W 4)$ | $2.803(7)(\times 2)$ |

Discussion. Fig. 1 reports a projection of the atomic arrangement along the $b$ axis.

The $\mathrm{P}_{6} \mathrm{O}_{18}$ ring anion. In the present arrangement the phosphoric ring is located around the twofold axis and so is built up of three independent $\mathrm{PO}_{4}$ tetrahedra. Up to now only two $\mathrm{P}_{6} \mathrm{O}_{18}$ ring anions have been observed with such an internal symmetry, the first in $\mathrm{Ca}_{2}\left(\mathrm{NH}_{4}\right)_{2} \mathrm{P}_{6} \mathrm{O}_{18} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (AverbuchPouchot, 1990) and the second, more recently, in $\mathrm{Ce}_{2} \mathrm{P}_{6} \mathrm{O}_{18} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (Bagieu-Beucher \& Rzaigui, 1991). The main geometrical features of the present ring are reported in Table 2. The $\mathrm{P}-\mathrm{P}$ distances and the $\mathrm{P}-\mathrm{O}-\mathrm{P}$ angles are those commonly measured in all condensed phosphoric anions. The P-P-P angles spread in a range of 98.95 to $116.38^{\circ}$ while in the two previous reported examples of $\mathrm{P}_{6} \mathrm{O}_{18}$ groups with a twofold internal symmetry these same ranges


Fig. 1. Projection along the $b$ axis of the atomic arrangement of $\mathrm{Ba}_{3} \mathrm{P}_{6} \mathrm{O}_{18} .8 \mathrm{H}_{2} \mathrm{O}$. The smaller empty circles are barium atoms, the larger ones represent water molecules.


Fig. 2. Upper part: projection of a ring along the $a$ axis. Lower part: projection of a ring along the $c$ axis.
are $87.8-116.1^{\circ}$ for $\mathrm{Ca}_{2}\left(\mathrm{NH}_{4}\right)_{2} \mathrm{P}_{6} \mathrm{O}_{18} .6 \mathrm{H}_{2} \mathrm{O}$ and $87.5-115.6^{\circ}$ for $\mathrm{Ce}_{2} \mathrm{P}_{6} \mathrm{O}_{18} .6 \mathrm{H}_{2} \mathrm{O}$. In spite of what might be suggested by Fig. 1, the present ring is far from being flat. Fig. 2 reports projections along b and $\mathbf{c}$ of an isolated anion showing clearly an organization made by two stages of tetrahedra.

The $\mathrm{BaO}_{n}$ polyhedra. Two crystallographically independent barium atoms are present in this arrangement, one in a general position and the other on the twofold axis. Within a range of $3 \AA$, the first has ten oxygen neighbours including three water molecules while the second has a more regular eightfold coordination including two water molecules. All these barium polyhedra are located in two layers approximately centred by planes $z=\frac{1}{4}$ and $\frac{3}{4}$. Inside these layers, through corner and edge sharing they build a tiling whose repetition unit is a ring of eight $\mathrm{BaO}_{n}$ polyhedra assembled to form a non-convex polygon. The $\mathrm{Ba}-\mathrm{Ba}$ distances in this twodimensional framework are rather short (4.3998 and $4.2079 \AA$ ). Table 2 gives the main interatomic distances in these two $\mathrm{BaO}_{n}$ polyhedra. Thus, in this atomic arrangement the cohesion between the two layers of barium polyhedra is performed through the external oxygen atoms of the large phosphoric ring anions.

Probably owing to the presence of the heavy cations, hydrogen atoms could not be located with a sufficient degree of accuracy. The drawings have been performed using the STRUPLO program (Fischer, 1985).

## References

Averbuch-Pouchot, M. T. (1989a). Z. Anorg. Allg. Chem. 570, 138-144.
Averbuch-Pouchot, M. T. (1989b). Acta Cryst. C45, 12751277.

Averbuch-Pouchot, M. T. (1990). Acta Cryst. C46, 20052007.

Averbuch-Pouchot, M. T. \& Durif, A. (1989). C. R. Acad. Sci. 309 II, 535-537.
Bagieu-Beucher, M. \& Rzaigui, M. (1991). Acta Cryst. C47, 1789-1791.
Enraf-Nonius (1977). Structure Determination Package. Version RSX-11M. Enraf-Nonius, Delft, The Netherlands.
Fischer, R. X. (1985). J. Appl. Cryst. 18, 258-262.
Lazarevski, E. V., Kubasova, L. V., Chudinova, N. N. \& Tananaev, I. V. (1980). Izv. Akad. Nauk SSSR Neorg. Mater. 16, 120-125.
Lazarevski, E. V., Kubasova, L. V., Chudinova, N. N. \& Tananaev, I. V. (1982a). Izv. Akad. Nauk SSSR Neorg. Mater. 18, 1550-1556.
Lazarevski, E. V., Kubasova, L. V., Chudinova, N. N. \& Tananaev, I. V. (1982b). Izv. Akad. Nauk SSSR Neorg. Mater. 18, 1544-1549.
Main, P., Lessinger, L., Woolfson, M. M., Germain, G. \& DECLERCQ, J.-P. (1977). MULTAN77. A System of Computer Programs for the Automatic Solution of Crystal Structures from X-ray Diffraction Data. Univs. of York, England, and Louvain, Belgium.


[^0]:    * Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Document Supply Centre as Supplementary Publication No. SUP 54605 ( 24 pp.). Copies may be obtained through The Technical Editor, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.

